


Optimal 3D Point Clouds from Mobile Laser Scanning



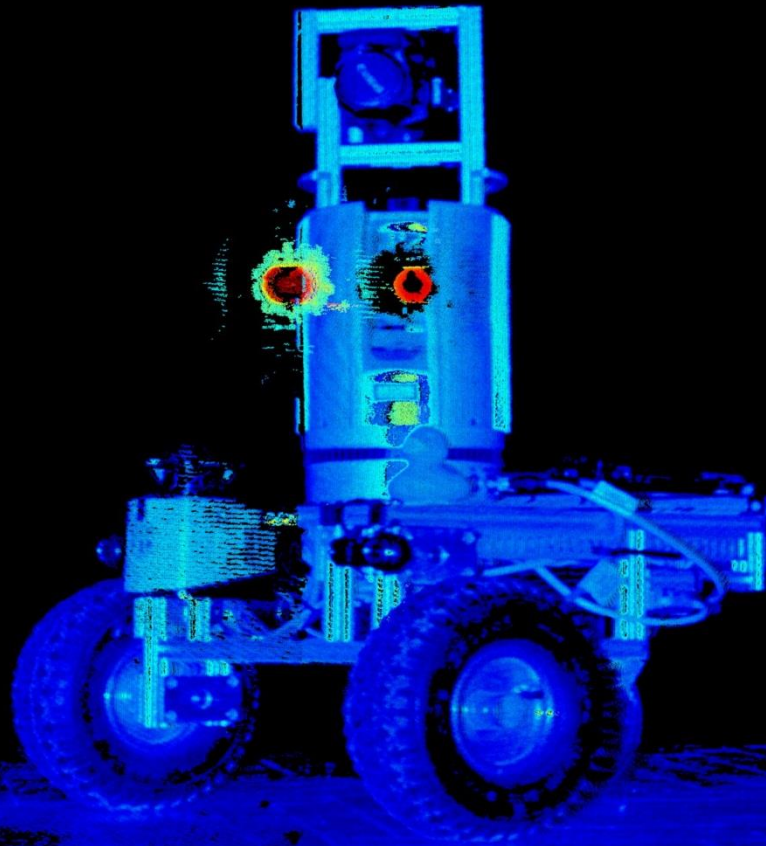
The image depicts how our robot Irma3D sees itself in a mirror. The laser looking into itself creates distortions as well as changes in intensity that give the robot a single eye, complete with iris and pupil.

Thus, the image is called "Self Portrait with Duckling".

Prof. Dr. Andreas Nüchter

About this talk...

(video)



Outline

- Introduction
- 3D Mapping with Mobile Robots
- Mobile Laser Scanning
 - Calibration
 - Semi-rigid Scan Matching
- Conclusion and Outlook



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The Ariadne Robot (2002/2003)

First, we used the 3D information for obstacle avoidance. Later of we did initial 3D mapping experiments.



The motion of the robot
3 DoF

(Video Crash) (Video NoCrash)

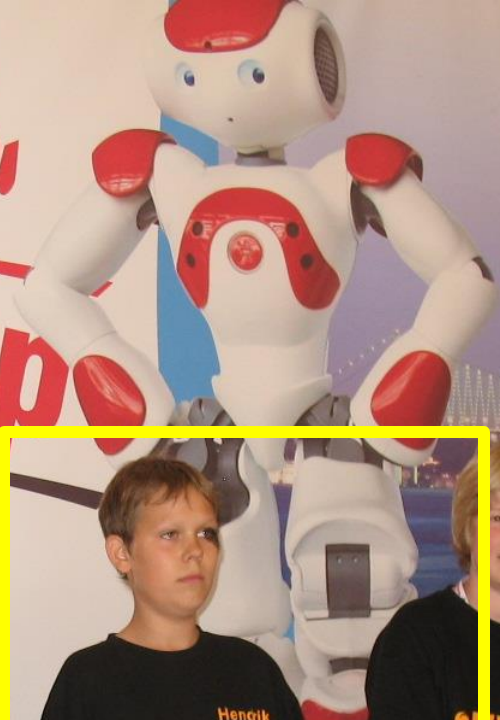




RoboCup

2011

-11 July
Istanbul -



HOSTED BY



ORGANIZAT



The Mobile Robot Irma3D (since 2010)

- Automation of 3D scanning



(video)

(video)

- Combination of terrestrial / kinematic laser scanning



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The ICP Algorithm

Scan registration Put two independent scans into one frame of reference

Iterative Closest Point algorithm [Besl/McKay 1992]

For prior point set M (“model set”) and data set D

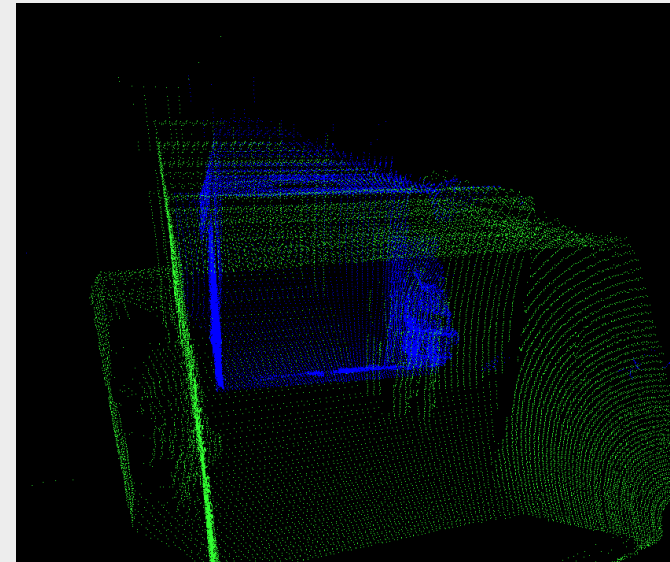
1. Select point correspondences
2. Minimize for rotation \mathbf{R} , translation \mathbf{t}

$$E(\mathbf{R}, \mathbf{t}) = \frac{1}{N} \sum_{i=1}^N \|\mathbf{m}_i - (\mathbf{R}\mathbf{d}_i + \mathbf{t})\|^2$$

3. Iterate 1. and 2.

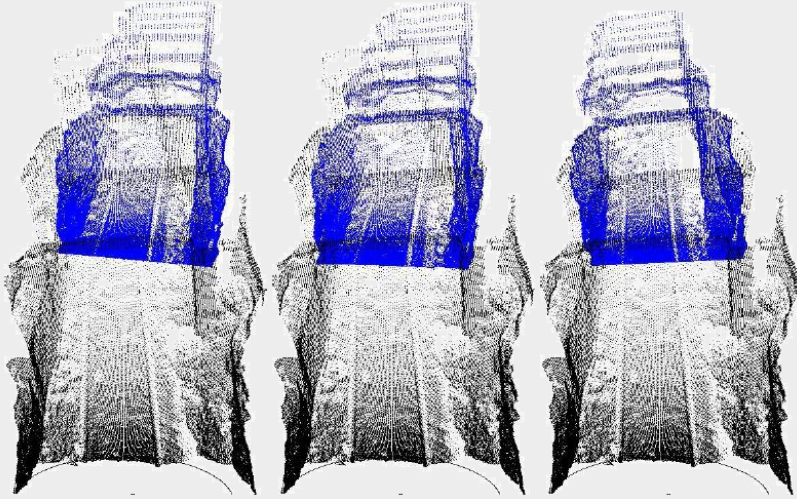
Four closed form solution for the minimization

- works in 3 translation plus 3 rotation dimensions



3D Mapping Examples

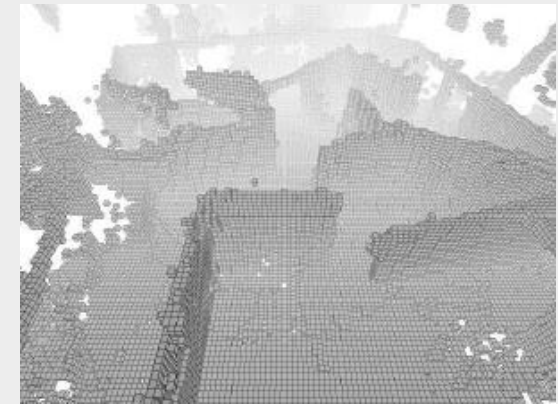
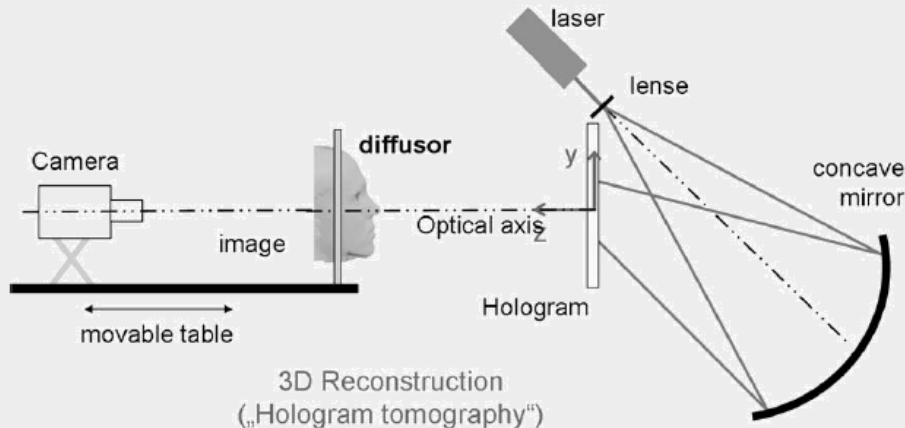
CMU 3D mapping of abandoned mines



RoboCup Rescue



3D reconstruction in the context of medical imaging



The Global ICP Algorithm

Scan registration Put two independent scans into one frame of reference

Iterative Closest Point algorithm [Besl/McKay 1992]

For prior point set M (“model set”) and data set D

1. Select point correspondences
2. Minimize for rotation \mathbf{R} , translation \mathbf{t}

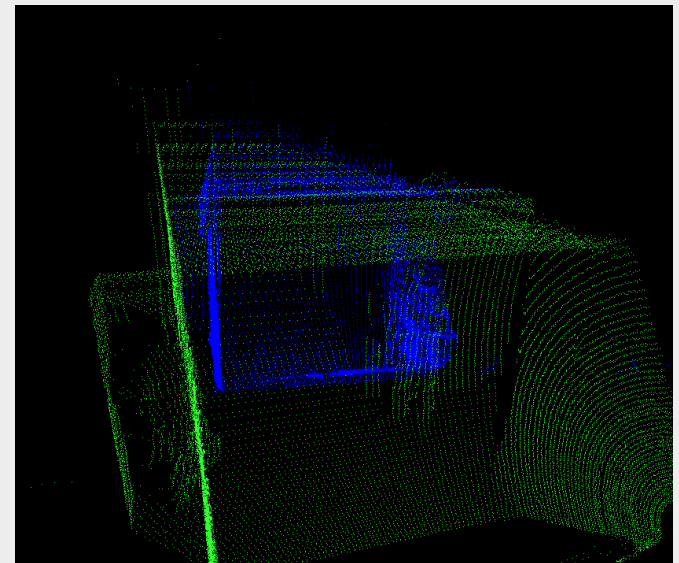
$$E(\mathbf{R}, \mathbf{t}) = \frac{1}{N} \sum_{i=1}^N \|\mathbf{m}_i - (\mathbf{R}\mathbf{d}_i + \mathbf{t})\|^2$$

3. Iterate 1. and 2.

Four closed form solution for the minimization

Global consistent registration

$$E = \sum_{j \rightarrow k} \sum_i |\mathbf{R}_j \mathbf{m}_i + \mathbf{t}_j - (\mathbf{R}_k \mathbf{d}_i + \mathbf{t}_k)|^2$$

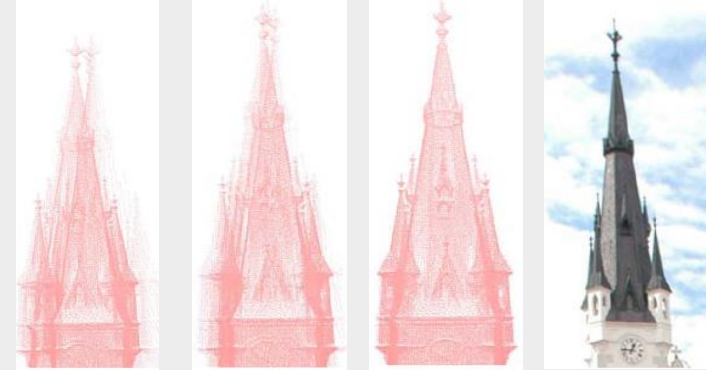


Example of high-precise registrations

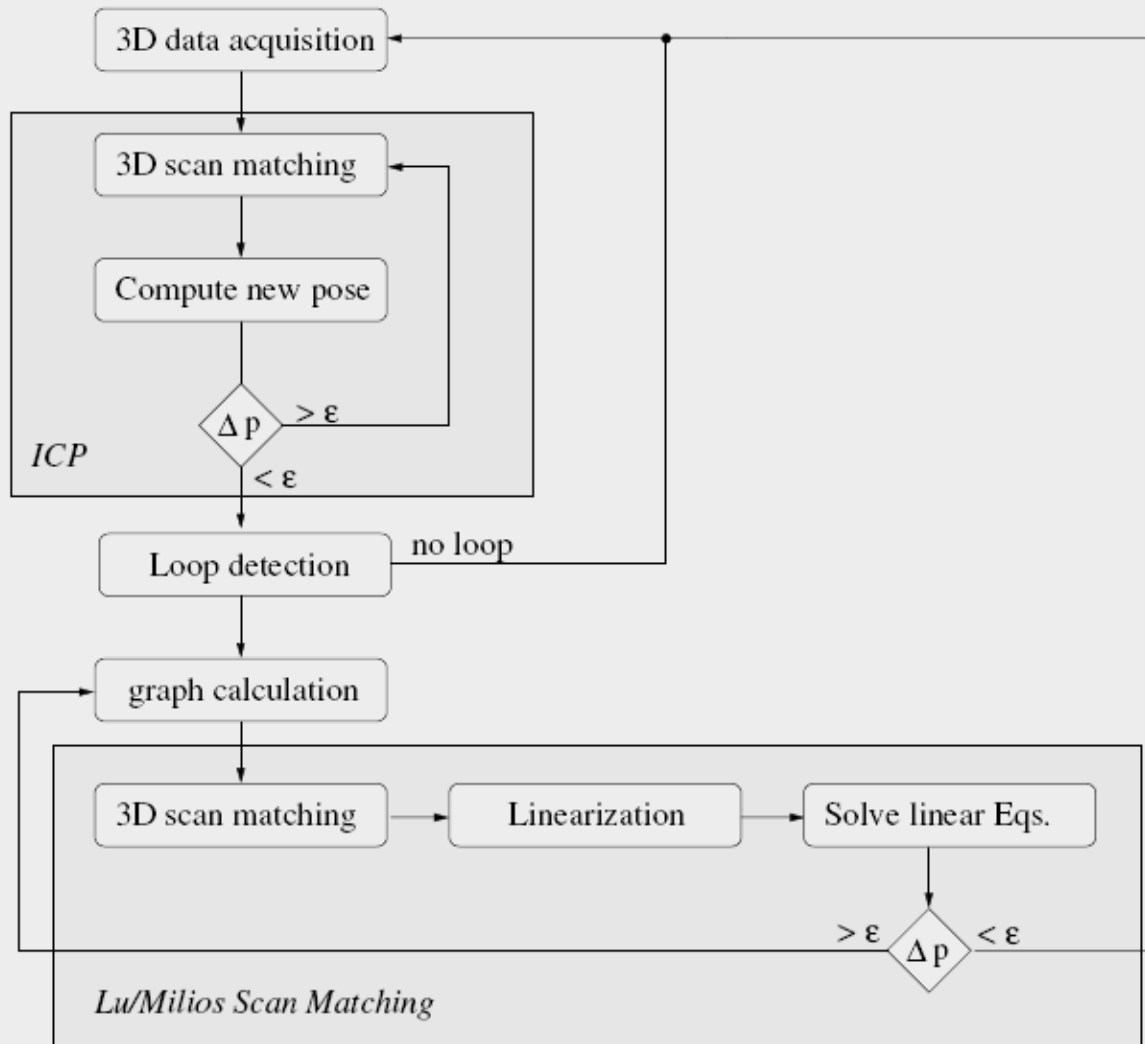
- Rieggl Laser Measurement GmbH

(Video courtesy of Rieggl)

(Video 1) (Video 2) (Video 3)

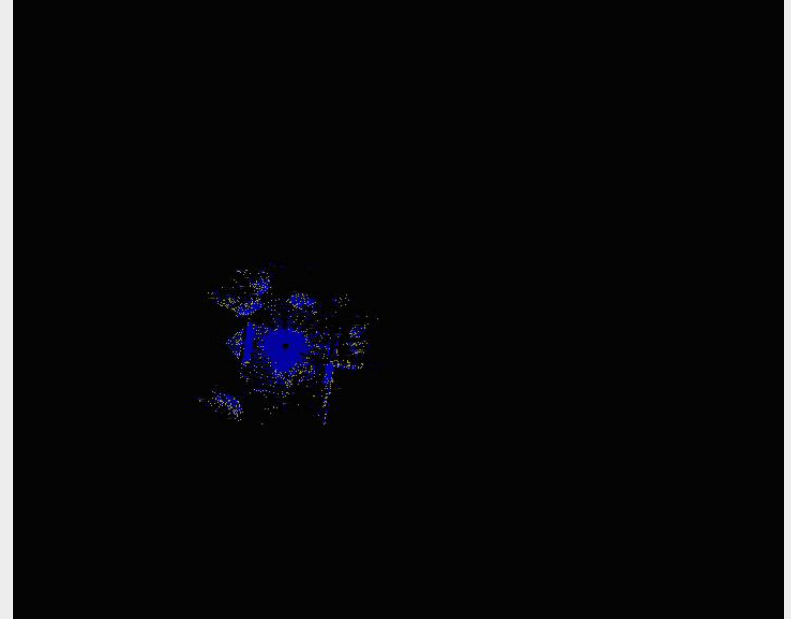


Closed Loop Detection and Global Relaxation



6D SLAM – Full Example

- Leibniz University Hannover (RTS)



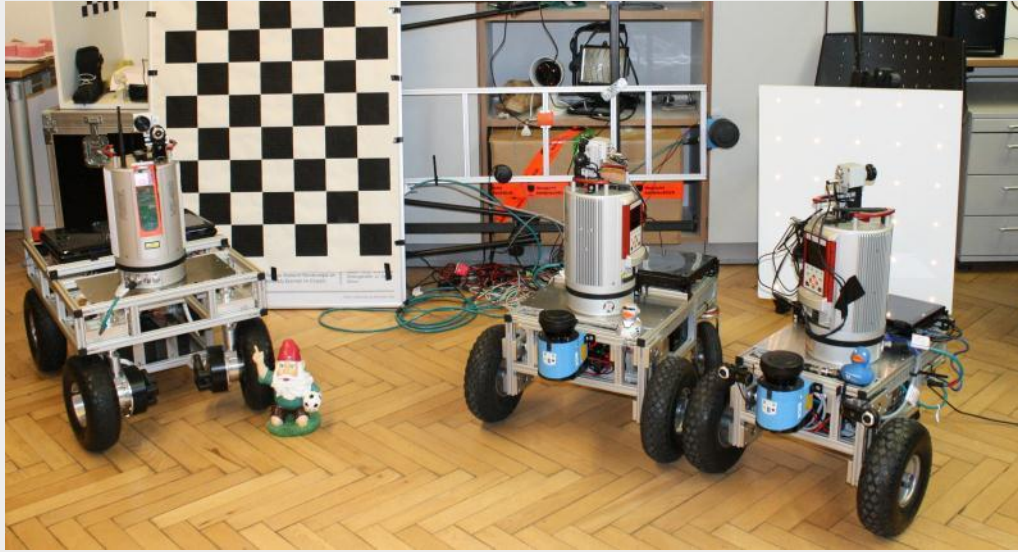
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Mobile Laser Scanning Systems

Experimental

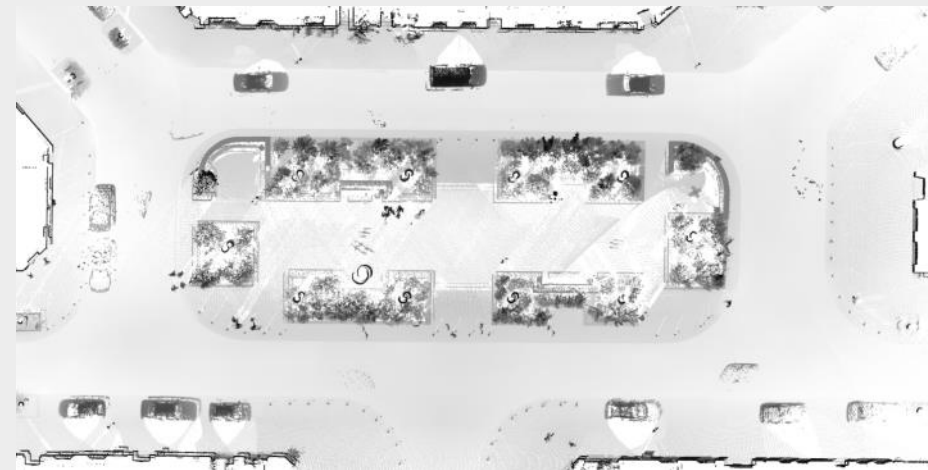


Professional



State of the Art

- For all sensors determine the position and orientation on the vehicle (calibration)
- Data Acquisition
- Extract the trajectory of the vehicle from the sensor data (Kalman-Filter)
- “Unwind” the laser measurements with the trajectory to create a 3D point cloud.



Automatic System Calibration

- Construct a calibration vector

$$\mathbf{C} = (a, w, \mathbf{W}_0, o_0, \dots, \mathbf{W}_n, o_n)$$

- Treat the „unwinding“ as a function $f(M, \mathbf{C})$
- The point cloud represents samples from a probability density function

$$d(\mathbf{l}) = \frac{1}{n} \sum_j^n G(\mathbf{l} - \mathbf{p}_j, \sigma^2 \mathbf{I})$$

- Simplified entropy measure

$$- \sum_i^n \sum_j^n G(\mathbf{p}_i - \mathbf{p}_j, 2\sigma^2 \mathbf{I})$$



Efficient Calibration

- Evaluating the entropy is in $O(n^2)$
- Reduction of the point cloud
 - n becomes smaller
 - Smaller contribution to the error function in the search space
- Reduction of point pairs
 - Consider only pairs with **minimal time difference**
 - Consider only **closest points**
- Minimization of the error function

$$\hat{\mathbf{C}} = \operatorname{argmax}_{\mathbf{C}} E(f(M, \mathbf{C}))$$

where
$$E(f(M, \mathbf{C})) = - \sum_i^n G(\mathbf{p}_i - \mathbf{q}_i, 2\sigma^2\mathbf{I})$$

is in $O(n \log n)$ (~20 minutes with Powel's algorithm)

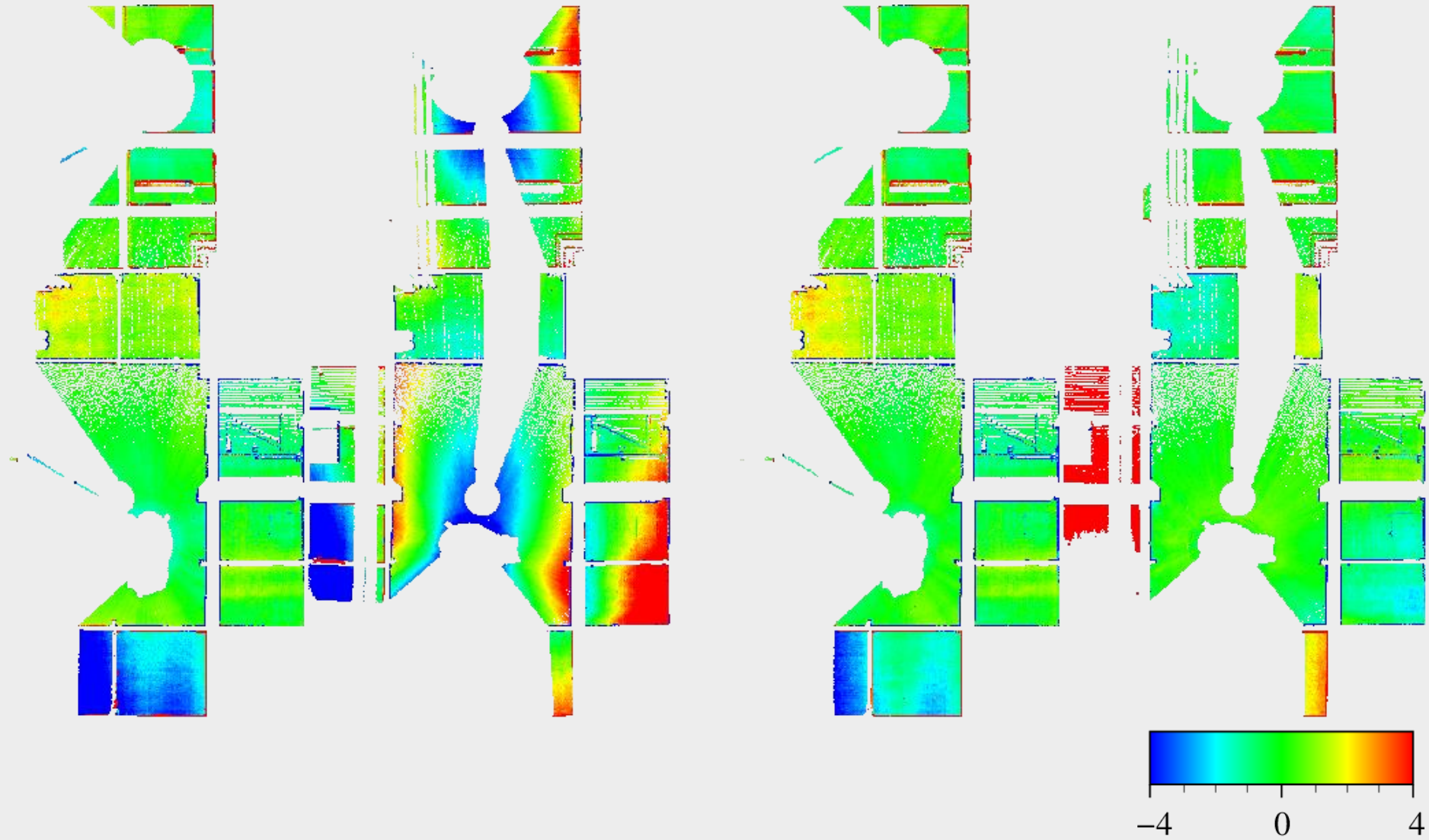
Calibration Experiment (1)



- Reference model: 3D plane model from terrestrial scanning
- Compare point cloud with model



Calibration Experiment (1)

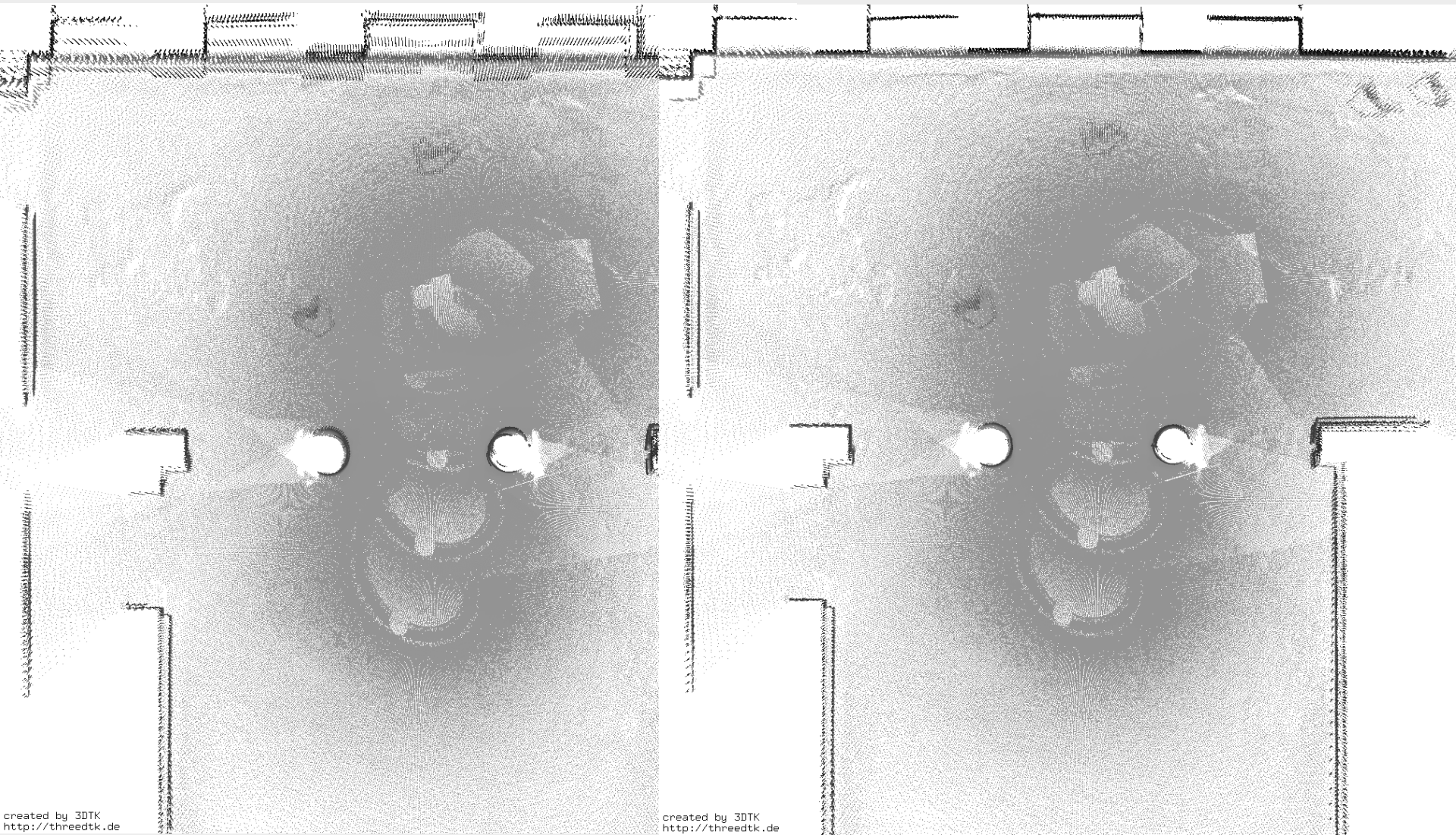


Calibration Experiment (2)

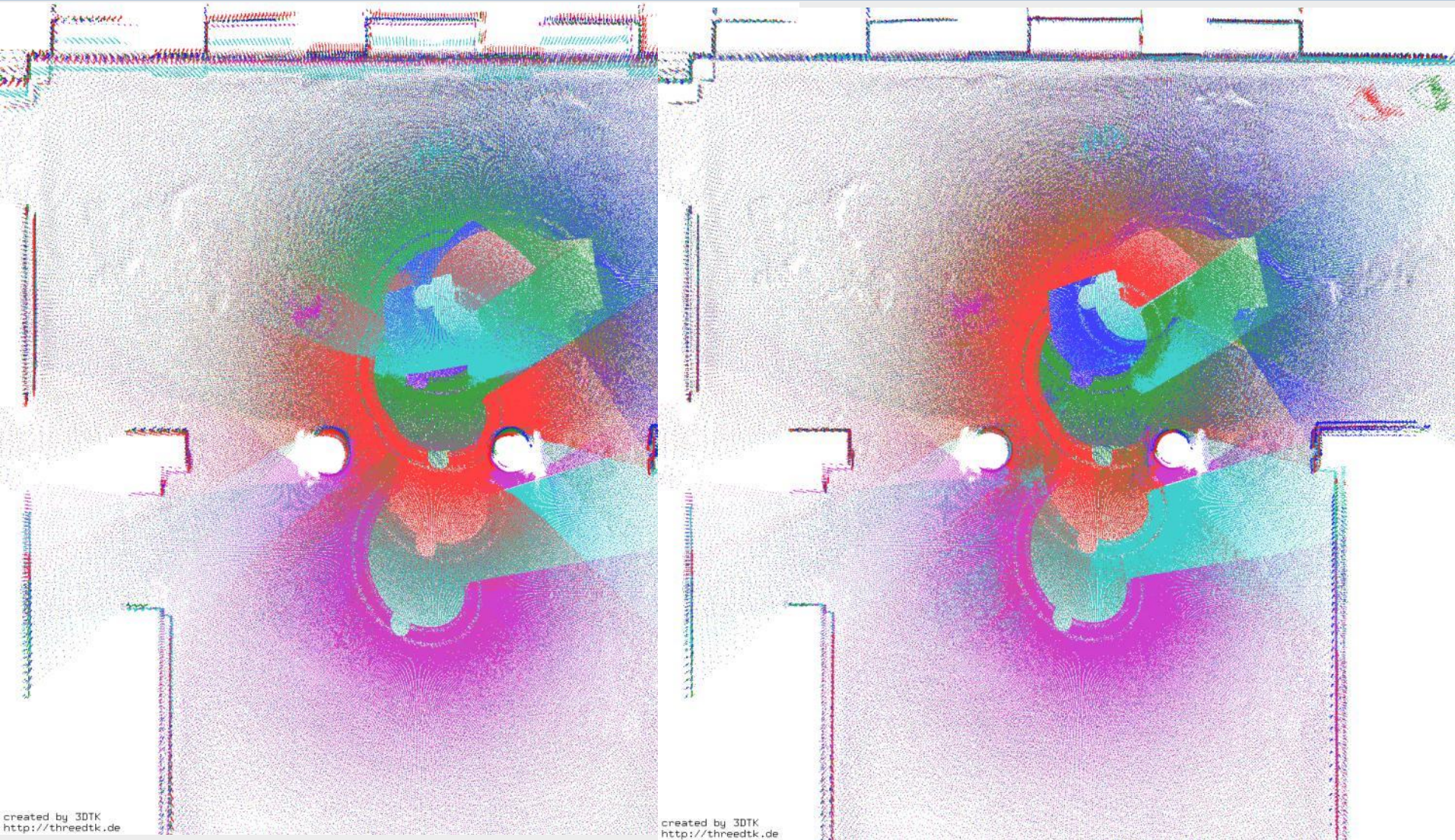
- Ostia Antica in Rom
- Environment less structured
- No ground truth model available



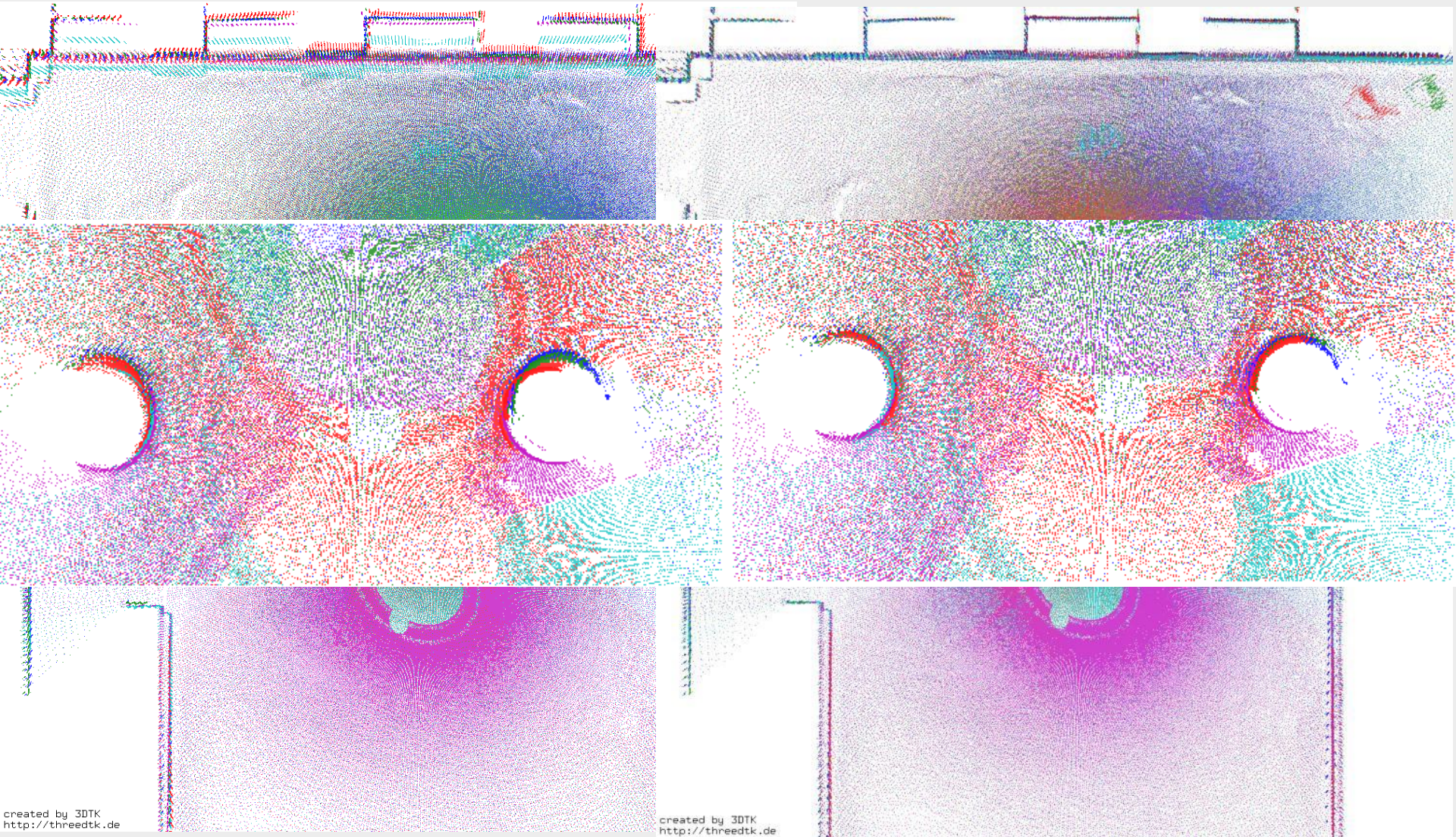
Calibration Experiment (2)



Calibration Experiment (2)



Calibration Experiment (2)



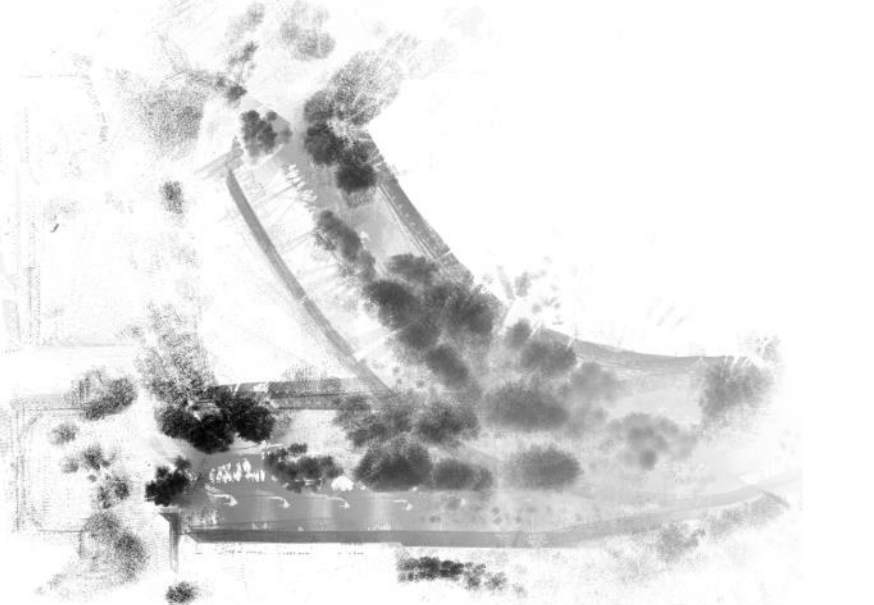
created by 3DTK
<http://threedtk.de>

created by 3DTK
<http://threedtk.de>



Further Sources of Errors

no GPS
„lousy“ IMU



bad GPS
no IMU



Semi-Rigid Registration

- Goal:
 - Optimize trajectory
 - No or only small time discretization (< 10 ms)
 - Ideal discretization at every point measurement
- Ansatz:
 - Extension of the global ICP algorithm / Graph-SLAM
- Modeling
 - Trajectory $T = \{\mathbf{V}_0, \dots, \mathbf{V}_n\}$
 - Every \mathbf{V}_i is a vehicle pose at time t_i
 - IMU / odometry estimate $\mathbf{V}_i \rightarrow \mathbf{V}_{i+1}$
 - GPS estimate $\mathbf{V}_0 \rightarrow \mathbf{V}_i$
 - Laser scanner / scan matching $\mathbf{V}_i \rightarrow \mathbf{V}_j$



Calculation of $\mathbf{V}_i \rightarrow \mathbf{V}_j$

- “Unwind” the laser measurements with the trajectory to create an initial 3D point cloud.
- Compute correspondences using a modified nearest-neighbor search
- Consider the following scenarios:

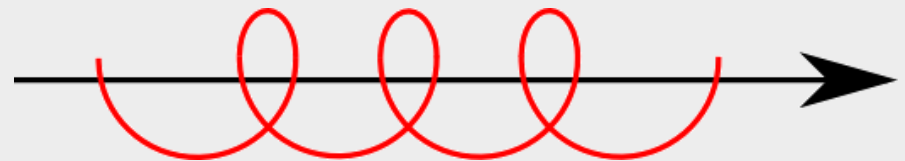
1 2D scanner



2 2D scanners



1 rot. 3D scanner



Optimization of the Trajectory

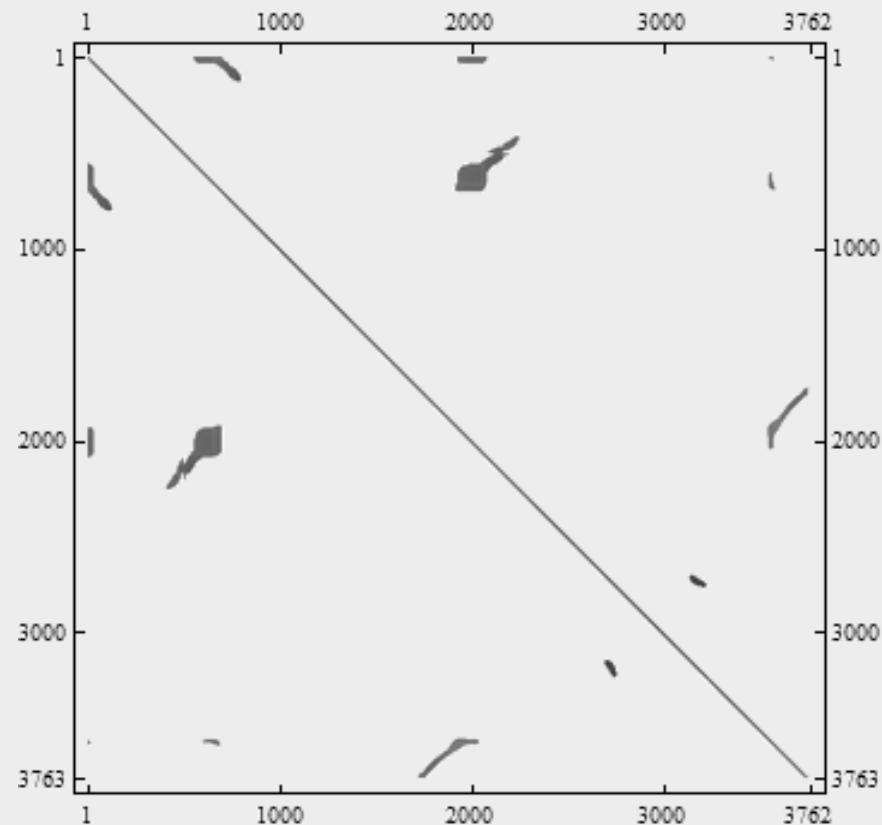
- Global error function

$$W = \sum_i \sum_j (\bar{\mathbf{V}}_{i,j} - (\mathbf{V}'_i - \mathbf{V}'_j)) \mathbf{C}_{i,j}^{-1} (\bar{\mathbf{V}}_{i,j} - (\mathbf{V}'_i - \mathbf{V}'_j))$$

- Minimization by

$$(\mathbf{H}^T \mathbf{C}^{-1} \mathbf{H}) \mathbf{V} = \mathbf{H}^T \mathbf{C}^{-1} \bar{\mathbf{V}}$$

- Solving by Sparse Choleskey Decomposition by T. Davis
- Also possible: global ICP



Overview: Algorithm Semi-Rigid SLAM

1. Calculate the pose estimates

$$\mathbf{V}_i \rightarrow \mathbf{V}_{i+1} \quad \text{and} \quad \mathbf{V}_0 \rightarrow \mathbf{V}_i$$

2. Extract a 3D point cloud from a current trajectory estimate and the system calibration

3. Calculate an oc-tree for storing the 3D points (including the time stamp)

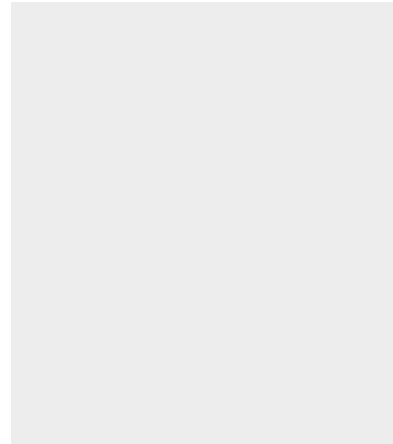
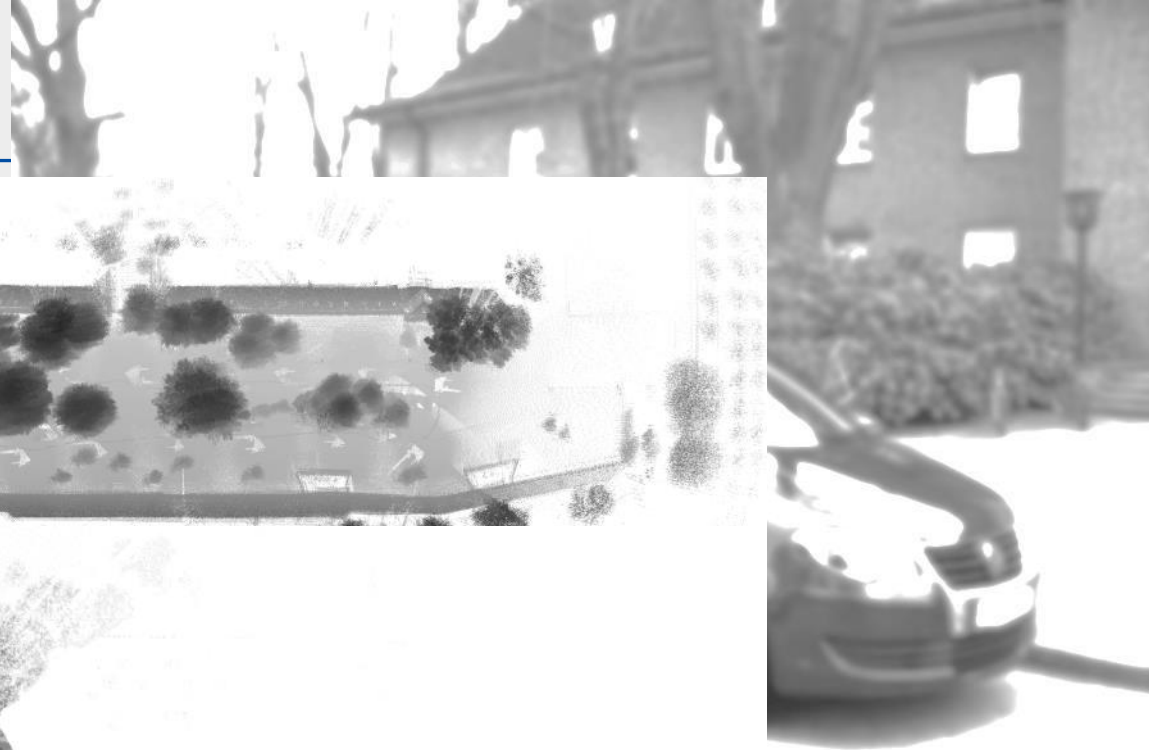
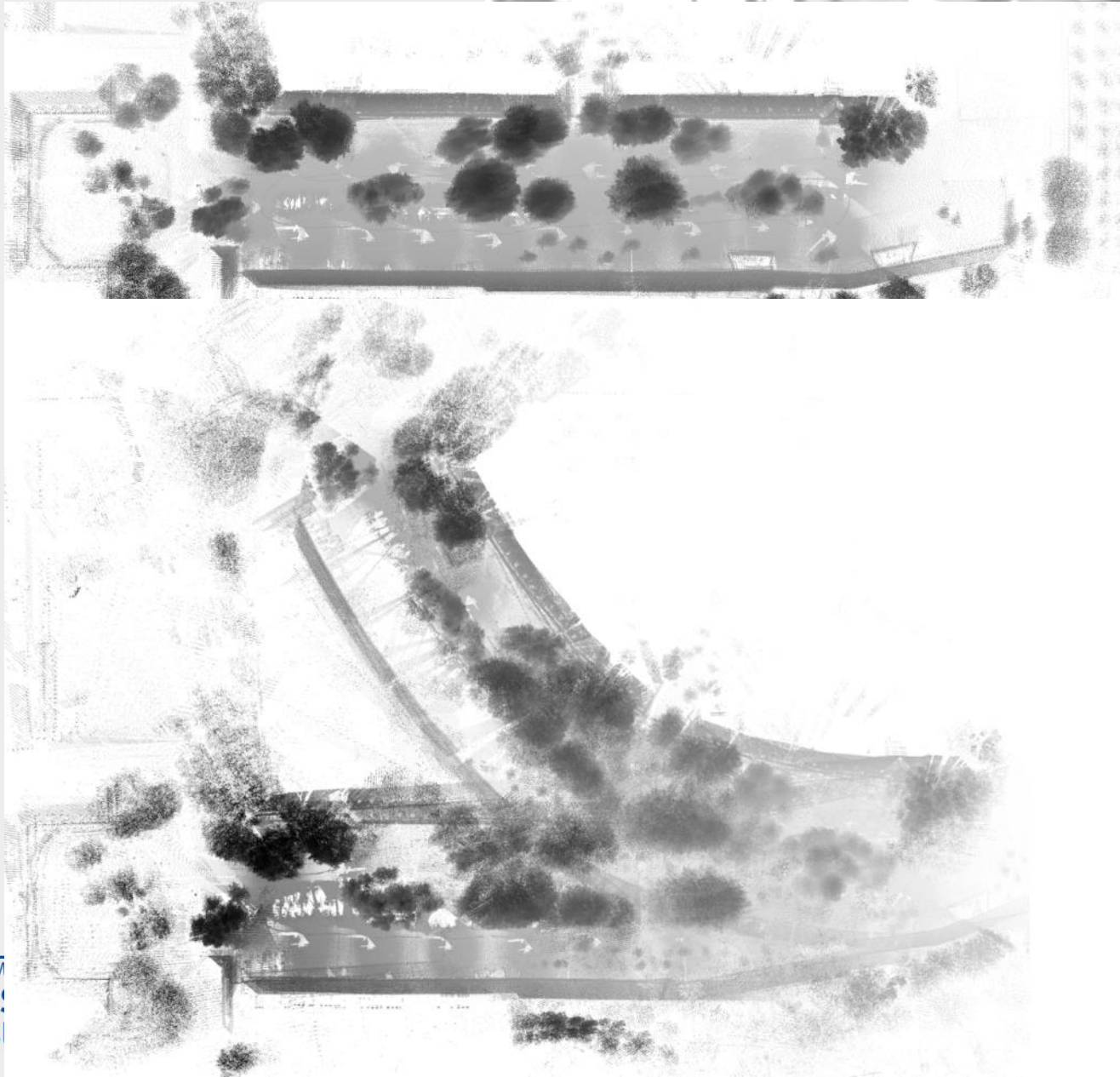
4. Compute closest points and an estimate for
 $\mathbf{V}_i \rightarrow \mathbf{V}_j$

5. Update the trajectory

6. Repeat step 2 – 5 until convergence

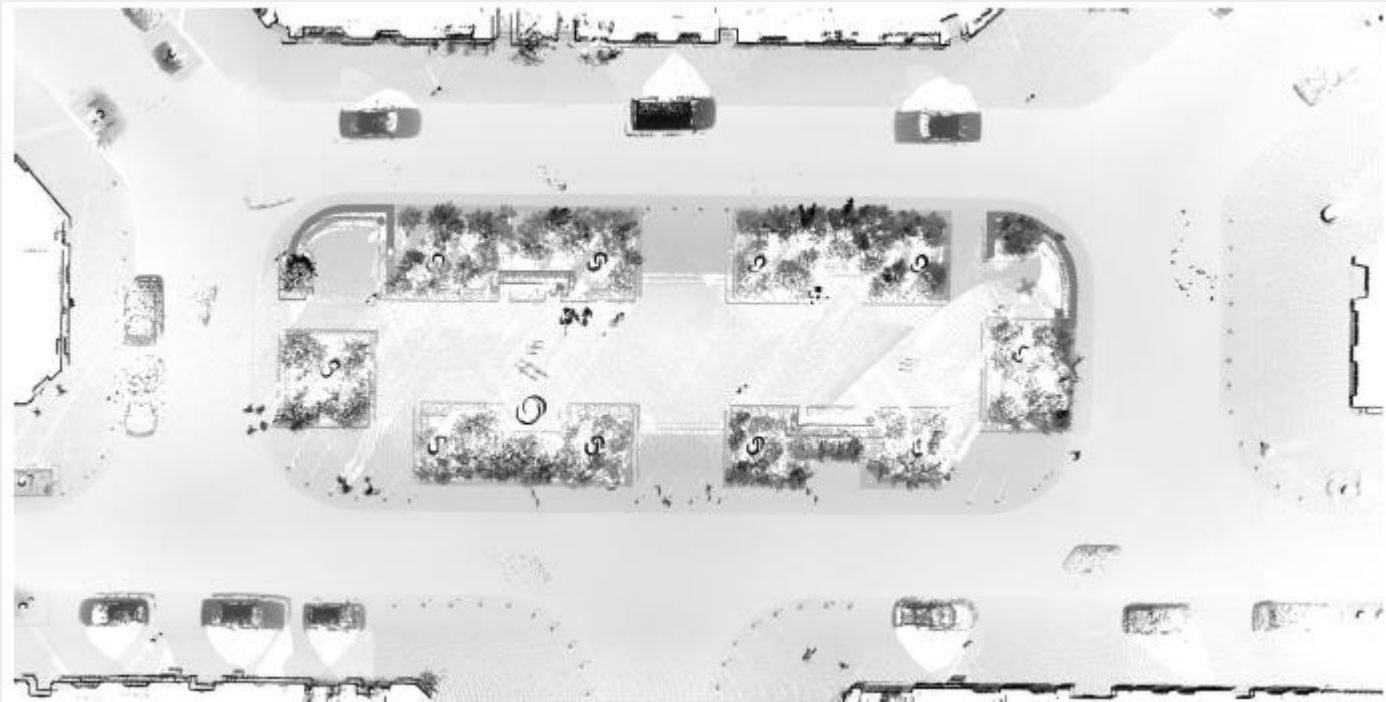


Experiment I



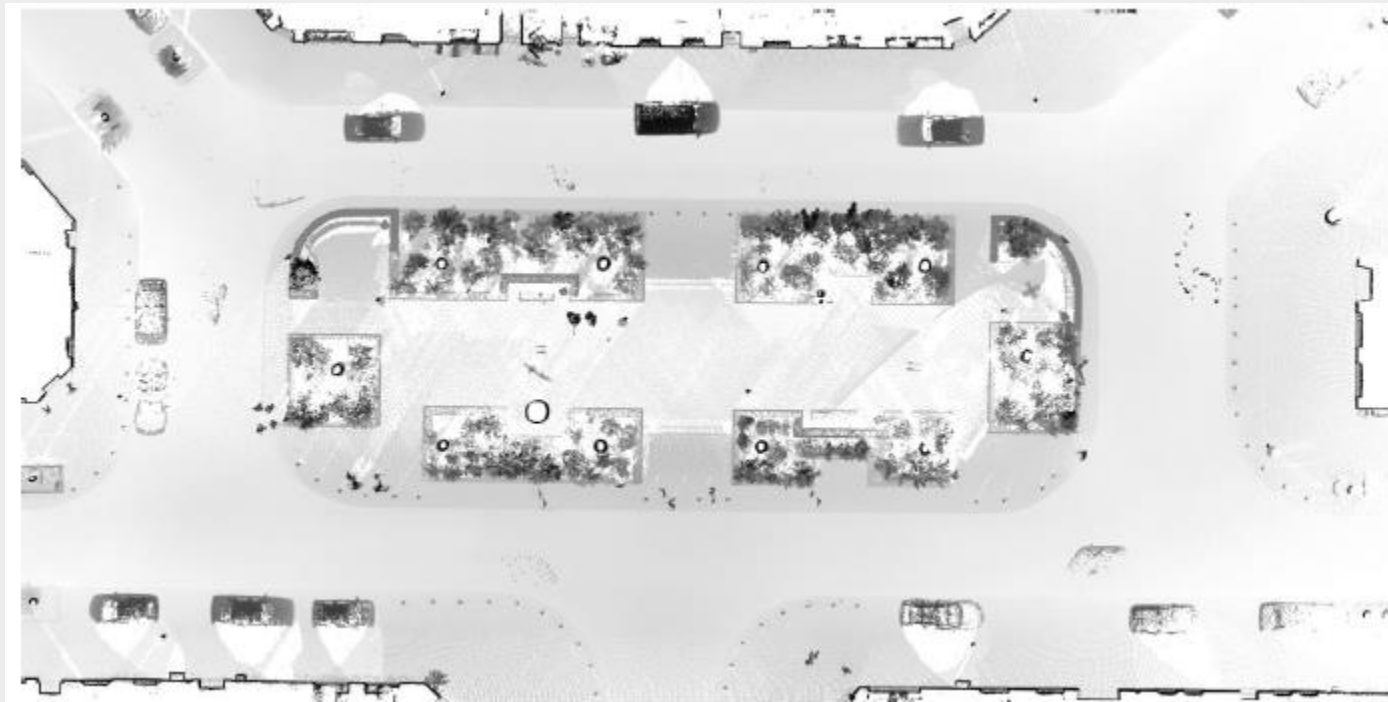
Experiment II

- Data and analysis done by TopScan GmbH, Rheine (Dr. Joachim Lindenberger)



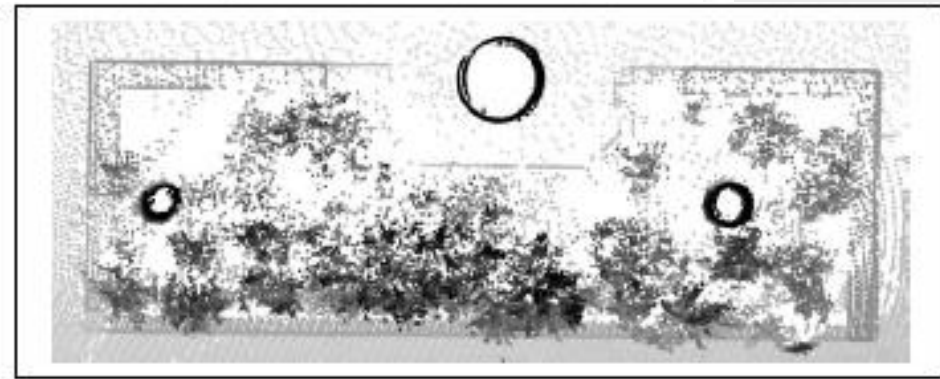
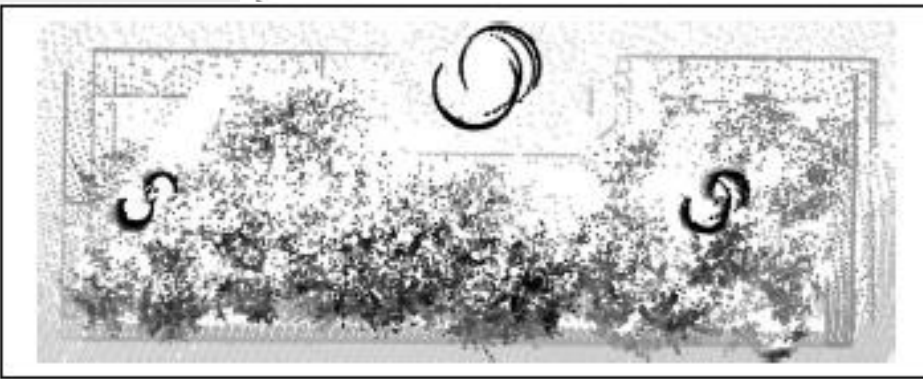
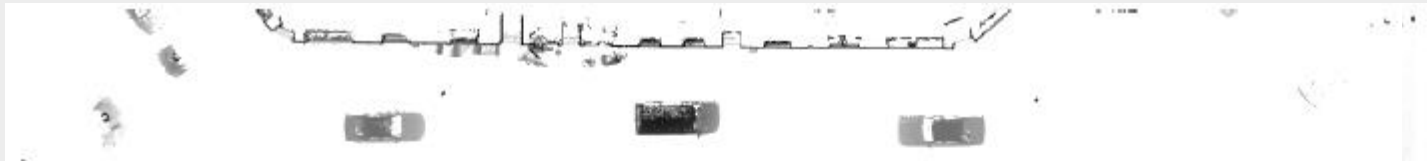
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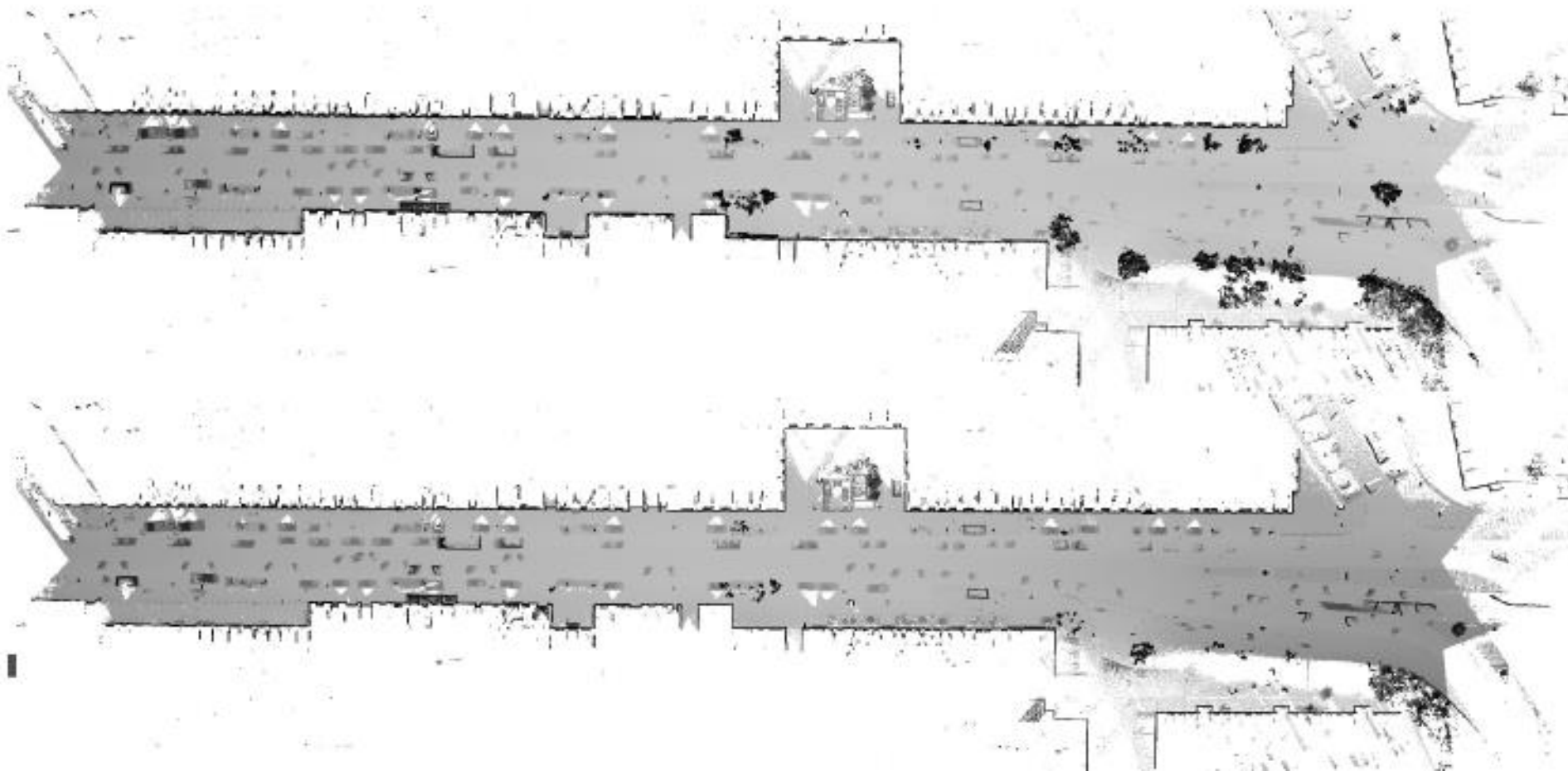


Experiment II

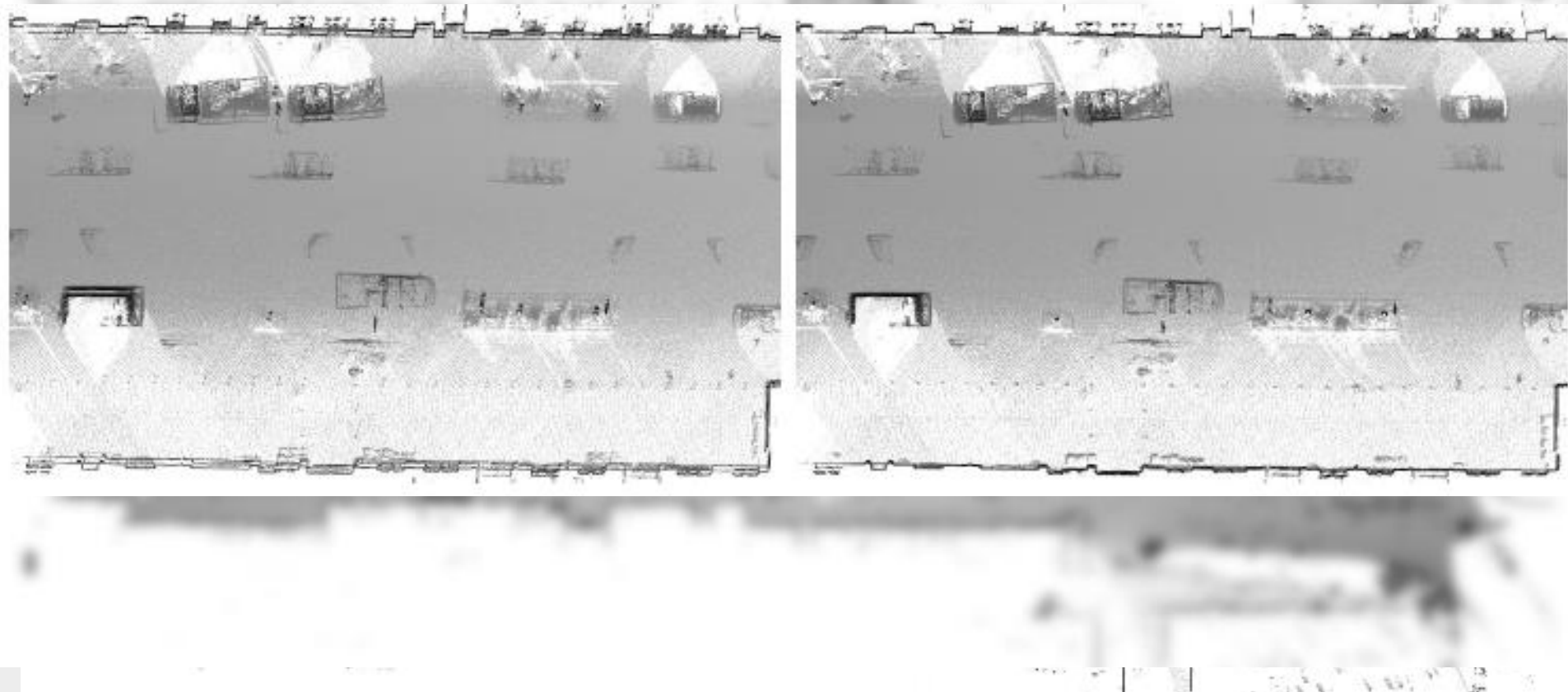
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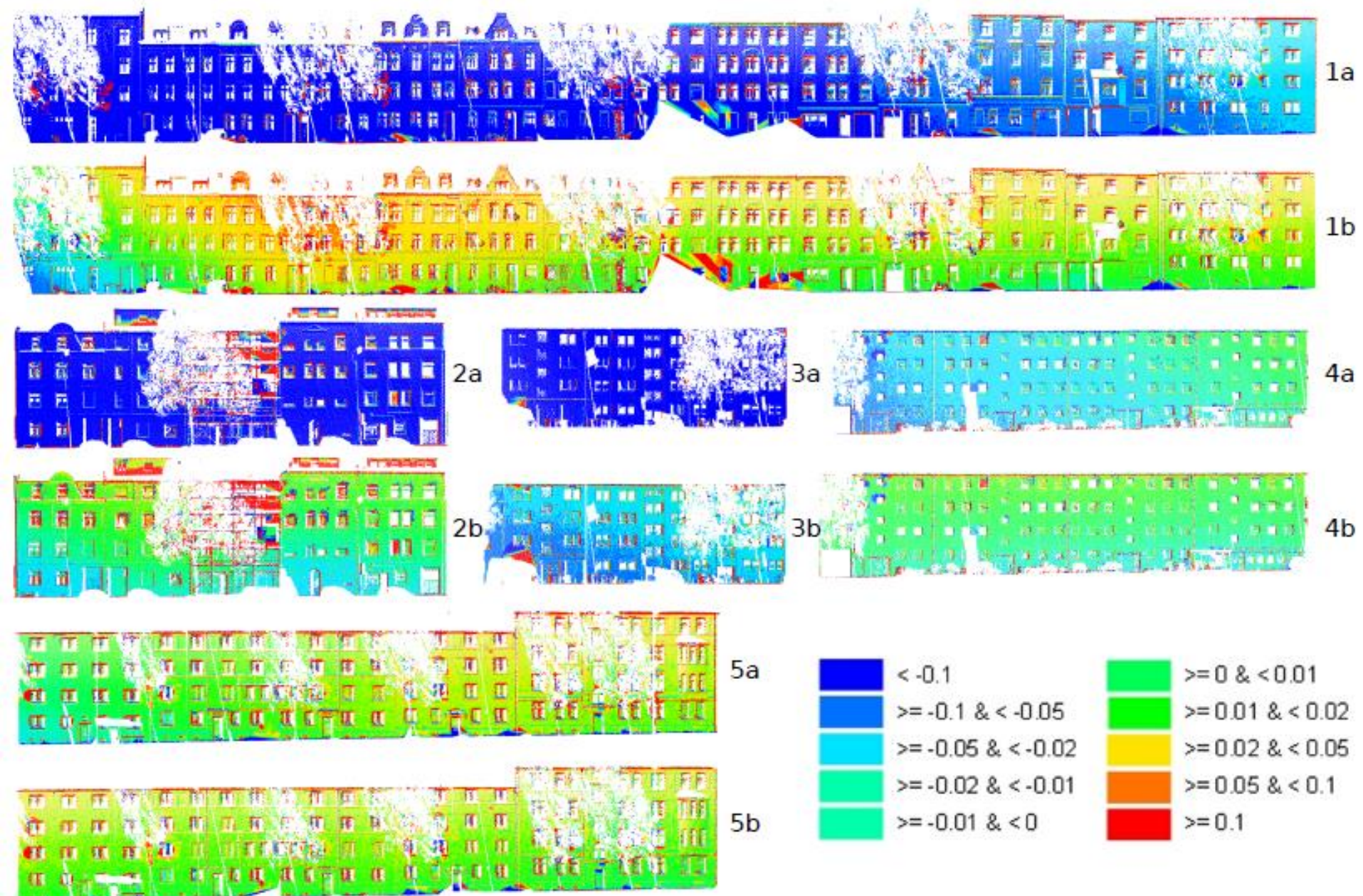
Experiment II



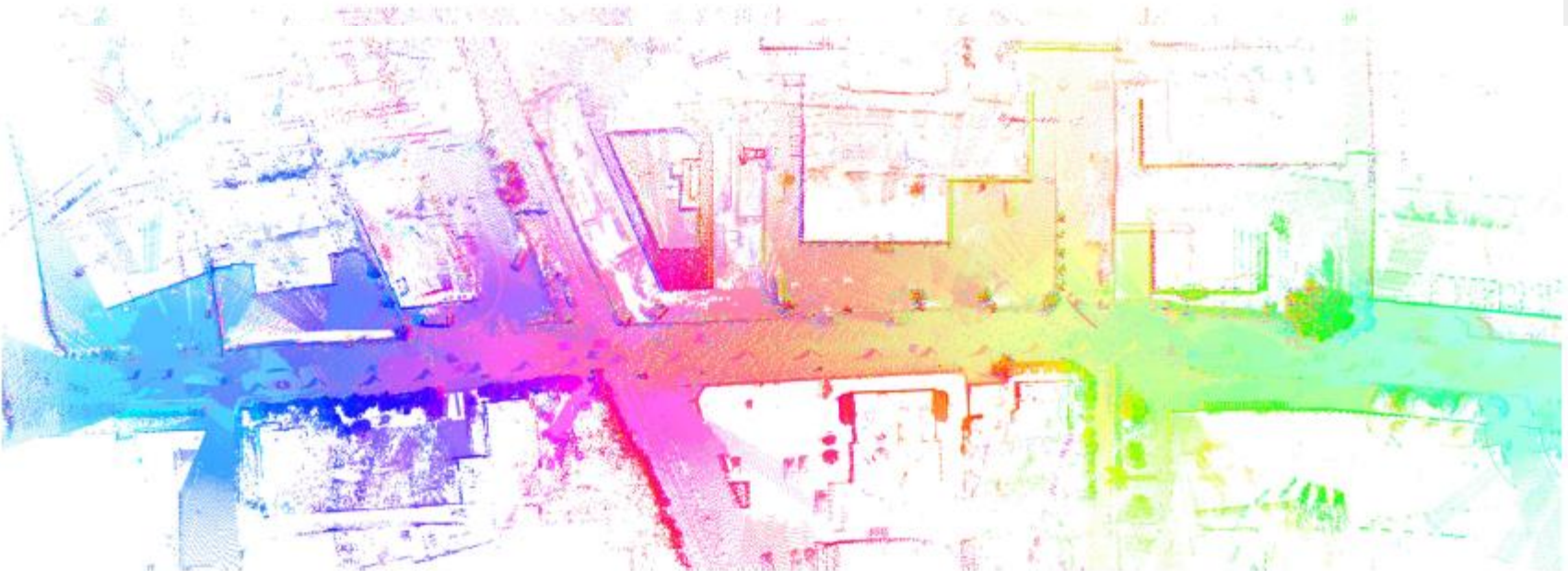
Experiment II



Experiment II

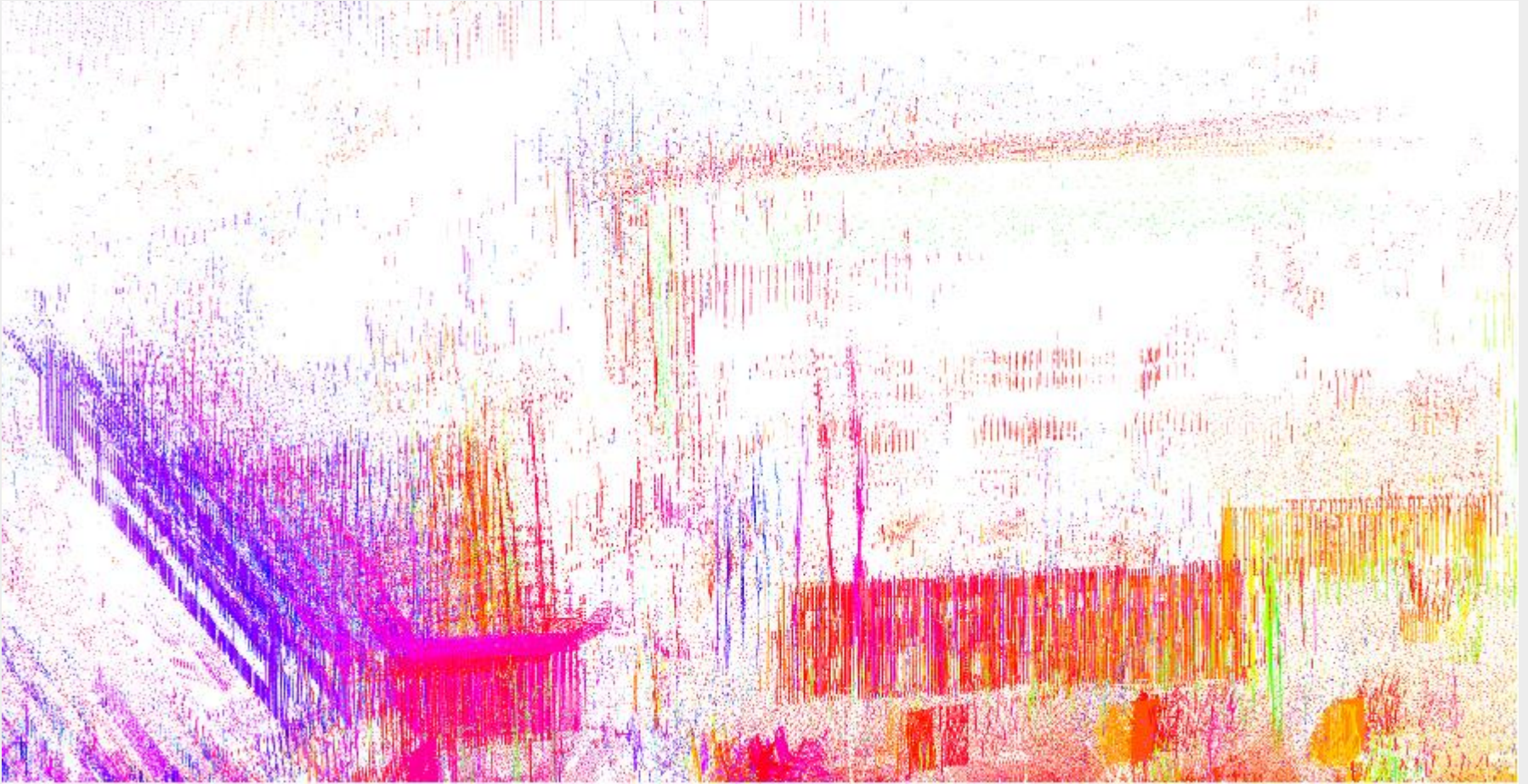


Experiment III



Experiment III

- Acquired by RiegI GmbH in Salzburg



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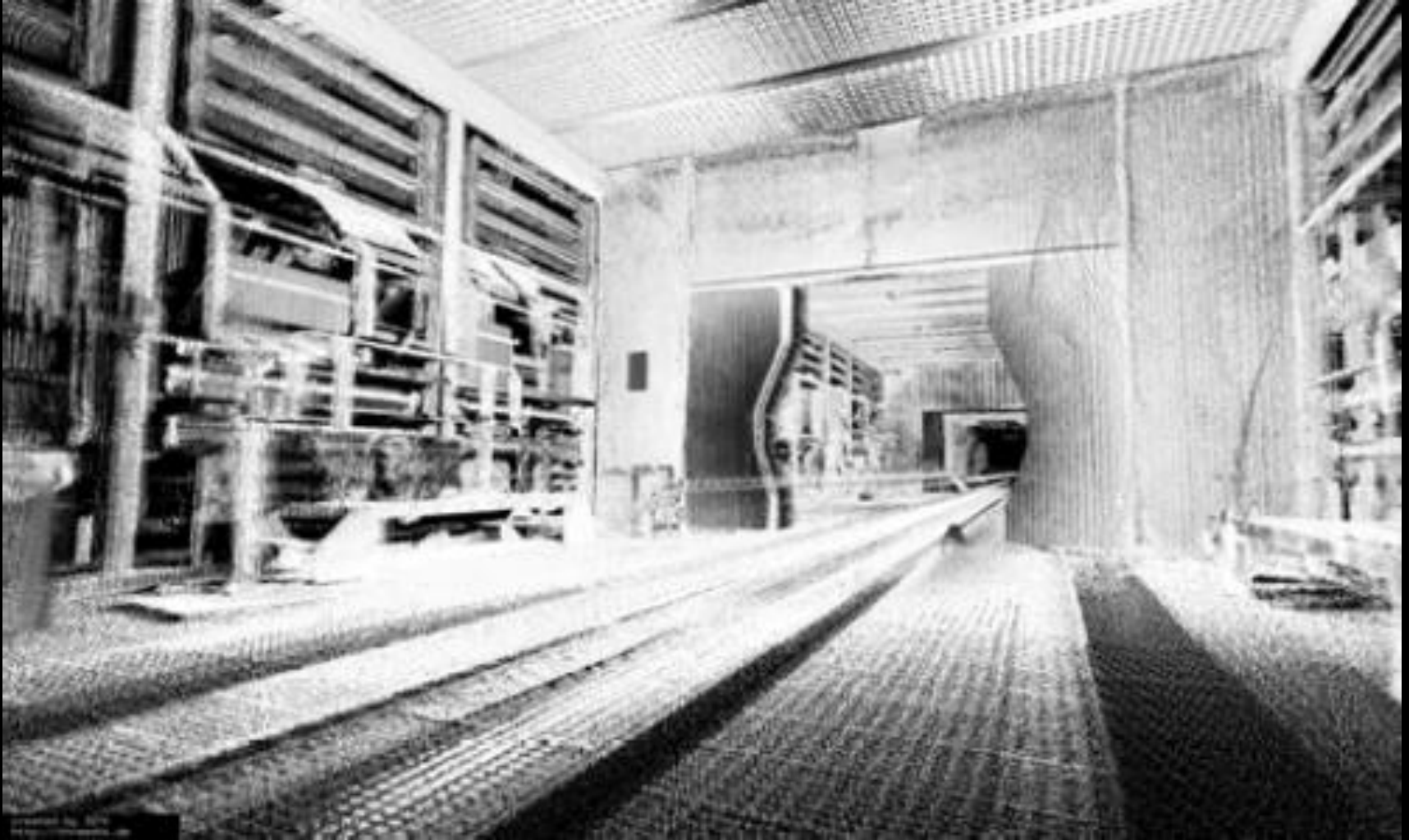


Summary and Outlook

- Efficient algorithms and data structures for processing 3D point clouds
- Global consistent scan matching
 - ⇒ Bundle Adjustment for 3D Point Clouds
 - ⇒ “Dense” method



Application: 3D Point Clouds at the Production Line



References

- Publications available at

www.nuechti.de

- Videos are online on our youtube channel

www.youtube.com/channel/UC7HAqZXI-jvMmBwoi4vDUew

www.youtube.com/user/AutomationAtJacobs

www.youtube.com/user/AndreasNuechter

- Large parts of our software is Open Source

3DTK – The 3D Toolkit

<http://slam6d.sourceforge.net>

